

## Isomer Ratios for Products of Photonuclear Reactions

### $^{121}\text{Sb}(\gamma,3n)^{118\text{m,g}}\text{Sb}$ and $^{121}\text{Sb}(\gamma,5n)^{116\text{m,g}}\text{Sb}$

Ia. Bezshyiko, O. Bezshyyko, L. Golinka-Bezshyyko, I. Kadenko  
Taras Shevchenko National University, Kyiv, Ukraine.

A. Dovbnya, S. Olejnik, G. Tuller, V. Vodin  
National Science Center “Kharkiv Institute of Physics & Technology” (NSC KIPT), Kharkiv, Ukraine.

V. Kushnir, V. Mitrochenko  
Research and Development Complex “Accelerator” of NSC KIPT, Kharkiv, Ukraine.

**Abstract.** Over the past several years various preequilibrium model approaches for nuclear reactions were developed. Diversified detailed experimental data in the medium excitation energy region for nucleus are needed for reasonable choice between these theoretical models. Lack of experimental data in this energy region does essentially limit the possibilities for analysis and comparison of different preequilibrium theoretical models. For photonuclear reactions this energy region extends between bremsstrahlung energies nearly 30–100 MeV. Experimental measurements and estimations of isomer ratios for products of photonuclear reactions with multiple particle escape on antimony have been performed using bremsstrahlung with energies 38, 43 and 53 MeV. Method of induced activity measurement was used. For acquisition of gamma spectra we used HPGe spectrometer with 20% efficiency and energy resolution 1.9 keV for 1332 keV gamma line of  $^{60}\text{Co}$ . Linear accelerator of electrons LU-40 was a source of bremsstrahlung. Energy resolution of electron beam was about 1% and mean current was within (3.8–5.3)  $\mu\text{A}$ .

## Introduction

Using high energy gamma-quanta as projectiles in nuclear reactions has some essential advantages for study of nuclear structure and nuclear reaction mechanisms. Indeed, gamma-quanta do not introduce large angular momentum into compound nucleus and additional contribution to excitation energy of compound nucleus due to binding energy of projectile is absent. In addition, the precise nondiscrete control of the gamma-quanta energy is possible.

Characteristics of photonuclear reactions are well studied in the energy region of Giant Dipole Resonance (GDR) and above the pion-producing threshold (PPT). The energy region between GDR and PPT (from about 30 to about 100 MeV) was studied to a smaller extent both theoretically and experimentally. The reason is due to small values of photonuclear reaction cross sections in this energy region and limited availability of high intensity quasi mono-energetic gamma ray sources with well controlled gamma-quanta energy.

During the last several years essential progress has been achieved in development of the new theoretical models for the photonuclear reactions and in improvement of the existing ones in the considered energy region. The quasi-deuteron model was further improved [Chadwick *et al.*, 1991], some new pre-equilibrium models have been developed for description of the multi-particle emission [Herman, *et al.* 2005; Talou *et al.*, 2006]. Permanently growing interest in Accelerator Driven Systems and progress in the design of high intensity quasi mono-energetic gamma-quanta sources [Gokhale *et al.*, 2006; <http://higs.tunl.duke.edu>.] also stimulates study of the photonuclear reactions above the GDR energy region. Very limited experimental data for the photonuclear reactions in the energy range (30–100) MeV for testing newly developed and available theoretical models was the major motivation for the present work.

The main purpose of this study is to obtain the experimental isomer ratios for nuclei  $^{118\text{m,g}}\text{Sb}$ ,  $^{116\text{m,g}}\text{Sb}$  as the products of the  $^{121}\text{Sb}(\gamma,3n)^{118\text{m,g}}\text{Sb}$  and  $^{121}\text{Sb}(\gamma,5n)^{116\text{m,g}}\text{Sb}$  reactions.

## Methodology

De-excitation time of nuclei by the  $\gamma$ -cascade irradiation usually does not exceed  $10^{-12}$  s [<http://www.nndc.bnl.gov/ensdf>]. In some cases transitions between levels of nucleus are suppressed due to the large difference of angular momentum of these levels involved and the nucleus can live long enough in a specific state called the isomer state. Usually these isomer state doesn't have large excitation energies and its angular momentum differs from a spin of the ground state by a few units of  $\hbar$ .

The isomer or ground levels with large values of spin are populated mainly from highly excited states with large spins values. Population of isomer or ground levels with smaller values of spin can occur mainly from highly excited states with small values of spins. Therefore investigations of relative populations of the isomer and ground states [Ishkhanov *et al.*, 1979; Gangrsky *et al.*, 1996] can be very useful to derive spins of highly excited levels and to study the de-excitation mechanisms via gamma emission.

For mono-energetic gamma beam with energy  $E$  the isomer ratio is determined as the cross sections ratio  $\frac{\sigma_m(E)}{\sigma_g(E)}$ , where  $\sigma_g(E)$  is the cross section of the photonuclear reaction leading to the ground state,  $\sigma_m(E)$  is the cross section for the same nucleus leading to the isomer state. Also the isomer ratio is often determined as a ratio of the cross section  $\sigma_H$  for state with higher spin to the cross section  $\sigma_L$  for state with lower spin:

$$\xi = \frac{\sigma_H(E)}{\sigma_L(E)}. \quad (1)$$

If a gamma beam is non-monoenergetic (this is the case for experiments with bremsstrahlung sources), the isomeric yield ratio is then being determined as:

$$d(E_{\max}) = \frac{Y_m}{Y_g}, \quad (2)$$

where the reaction yield is given by

$$Y_{m,g} = N_t \int_{E_{thr}^{m,g}}^{E_{\max}} \sigma_{m,g}(E) \cdot W(E, E_{\max}) dE, \quad (3)$$

$N_t$  —number of the target nuclei,  $Y_{m,g}$  —reaction yield for nucleus in the isomer (m) or ground (g) state,  $E_{\max}$  —maximal gamma energy,  $W(E, E_{\max})$  —bremsstrahlung spectrum,  $\sigma_i(E)$  with  $i = m, g$  —the reaction cross section for nucleus to be formed in meta-stable (ground) state for gamma energy  $E$ ,  $E_{thr}^i$ ,  $i = m, g$  —the energy threshold of the reaction leading to the meta-stable (ground) state.

Production of isomeric pair and its decay can be described by the following differential equation system:

$$\begin{cases} \frac{dN_m}{dt} = Y_m - \lambda_m \cdot N_m \\ \frac{dN_g}{dt} = Y_g - \lambda_g \cdot N_g + p \cdot \lambda_m \cdot N_m \end{cases}, \quad (4)$$

where  $N_i$  —population of  $i$ -state ( $i = m$  —isomer state,  $i = g$  —ground state),  $Y_i$  —reaction yield according to (3),  $\lambda_m$ ,  $\lambda_g$  —decay constants for isomer and ground state,  $p$  —branching factor (transition probability from isomer to ground state) [Vanska *et al.*, 1981; Kolev *et al.*, 1995]. The equation system is valid under such conditions: gamma-quanta flux is time invariable; contribution

from interfering reaction may be considered as negligible; simple decay scheme, when the isomer level decays by gamma transition to the ground state in competition with  $\beta$ -decay and the ground state decays by  $\beta$ -decay branch. Solution of system (4) is:

$$\begin{cases} \frac{S_m}{C \cdot \varepsilon \cdot f_m} = Y_m \Lambda_3 \Lambda_6 \Lambda_9 \\ \frac{S_g}{C \cdot \varepsilon \cdot f_g} = Y_g \Lambda_2 \Lambda_5 \Lambda_8 + \\ + Y_m (\Lambda_1 \Lambda_5 \Lambda_8 + \Lambda_3 \Lambda_4 \Lambda_8 + \Lambda_3 \Lambda_6 \Lambda_7) \end{cases}, \quad (5)$$

where  $S_i$ ,  $i = g, m$ —photo-peak area (in the gamma spectrum of the activation products), coefficient  $C$  includes self-absorption factor, true coincidence effects of cascade gammas and other effects,  $\varepsilon$ —full efficiency of gamma detection for the analysed gamma-line;  $f_i$ ,  $i = g, m$ —quantum yield of gamma-line for  $i$ -state decay (transition probability for this line); coefficients  $\Lambda_j$ ,  $j = 1, 9$  are defined by  $t_1$ ,  $t_2$ ,  $t_3$ —irradiation time, cooling time and measurement time, respectively:

$$\begin{aligned} \Lambda_1 &= \frac{p}{\lambda_g} \left[ 1 - \frac{\lambda_m \lambda_g}{\lambda_m - \lambda_g} \left( \frac{e^{-\lambda_g t_1}}{\lambda_g} - \frac{e^{-\lambda_m t_1^g}}{\lambda_m} \right) \right] \\ \Lambda_2 &= \frac{1}{\lambda_g} \left( 1 - e^{-\lambda_g t_1} \right), \quad \Lambda_3 = \frac{1}{\lambda_m} \left( 1 - e^{-\lambda_m t_1} \right) \\ \Lambda_4 &= p \frac{\lambda_m}{\lambda_m - \lambda_g} \left( e^{-\lambda_g t_2} - e^{-\lambda_m t_2} \right) \\ \Lambda_5 &= e^{-\lambda_g t_2}, \quad \Lambda_6 = e^{-\lambda_m t_2} \\ \Lambda_7 &= p \left[ 1 - \frac{\lambda_m \lambda_g}{\lambda_m - \lambda_g} \left( \frac{e^{-\lambda_g t_3}}{\lambda_g} - \frac{e^{-\lambda_m t_3}}{\lambda_m} \right) \right] \\ \Lambda_8 &= 1 - e^{-\lambda_g t_3}, \quad \Lambda_9 = 1 - e^{-\lambda_m t_3} \end{aligned}$$

As a result, the following expression is obtained

$$F = Y'_m X + Y'_g, \quad (6)$$

where  $F$  and  $X$  are defined as

$$F = \frac{S}{\varepsilon \cdot f_g \Lambda_2 \Lambda_5 \Lambda_8}, \quad X = \frac{(\Lambda_1 \Lambda_5 \Lambda_8 + \Lambda_3 \Lambda_4 \Lambda_8 + \Lambda_3 \Lambda_6 \Lambda_7) + \frac{f_m}{f_g} \Lambda_3 \Lambda_6 \Lambda_9}{\Lambda_2 \Lambda_5 \Lambda_8}, \quad (7)$$

with  $S = S_g + S_m$  peak area sum,  $Y'_{m,g} = C Y_{m,g}$ —values, proportional to reaction yields.

In this particular case isomer yield ratio was calculated by fitting the experimental data (X, F) using expression (6).

Experimentally, the method of induced activity was applied to obtain the isomer ratios. Irradiations of Sb target have been carried out with bremsstrahlung endpoint energies within the region (38–53) MeV. Linear accelerator LU-40 (Research and Development Complex “Accelerator” NSC KIPT) was used as a source of fast electrons [Dovbnya *et al.*, 2006]. Instability of electron beam intensity was within 2%. Inner monitor of electron beam was calibrated by values from Faraday cup of the magnetic analyser, placed at the accelerator outlet. The tantalum converter with 1.05 mm thickness was placed on the exit window of the accelerator facility, close to which the cylindrical aluminium gamma absorbers (thickness 5.5 and 10 cm) were installed. Diameter of beam spot on the conversion target was less than 9 mm. Energy of electron beam was determined using magnetic analyser and was double checked in the low energy region by considering the photonuclear reaction thresholds. A distance between tantalum converter and absorber was 2 cm, between tantalum converter and target – 20 cm. We used metallic antimony target with natural isotopic abundance to study the reaction  $^{121}\text{Sb}(\gamma,3n)^{118\text{m,g}}\text{Sb}$  and the reaction  $^{121}\text{Sb}(\gamma,5n)^{116\text{m,g}}\text{Sb}$ . Irradiation time for every sample was 5 min. Then within (3 – 8) seconds the irradiated sample was moved with pneumatic transfer system to the measurement area. HPGe detector with the energy resolution  $<2.0$  keV for  $^{60}\text{Co}$   $\gamma$ -line 1332 keV was used to acquire the instrumental gamma-ray spectra of the activation products as a set of serial measurements with various time periods. Cooling times varied from 5 seconds to few hours. Distances between sample and detector (dozens centimetres just after irradiation and few centimetres at the end of measurement period) were chosen to optimize both statistics and time restrictions when large contribution of interfering reactions took place, minimum distance was restricted by condition of negligible contribution of cascade gammas summing. Efficiency calibration of spectrometer was carried out for each detector-to-sample distance. The efficiency-energy dependence in double logarithmic scale showed a good quality and linearity in the energy range of interest, with deviations between experimental data and linear fitted values not exceeding 2%.

## Results and discussion

Isomer ratios were obtained as  $IR(E_\gamma) = \frac{Y_H(E_\gamma)}{Y_L(E_\gamma)}$ , where  $Y_H(E_\gamma)$  is the reaction yield for the state of final nucleus with larger angular momentum (meta-stable state),  $Y_L(E_\gamma)$  is the reaction yield for the state of final nucleus with smaller angular momentum (ground state). We used the decay scheme of the  $^{116\text{m,g}}\text{Sb}$  and  $^{118\text{m,g}}\text{Sb}$  nuclei from [<http://www.nndc.bnl.gov/ensdf>].

Examples of spectra from the induced activities for the antimony target are shown in Fig. 1.(left) The gamma line 1293,5 keV (common line for EC+ $\beta^+$  decay of the ground and isomer states) were used to obtain the isomer ratio for  $^{116\text{m,g}}\text{Sb}$  and the gamma line 1097 keV ( $\gamma$ -decay of the isomer state) was used to account contribution of  $^{116\text{m,g}}\text{In}$  (reaction  $^{121}\text{Sb}(\gamma,\alpha)^{116\text{m,g}}\text{In}$ ).

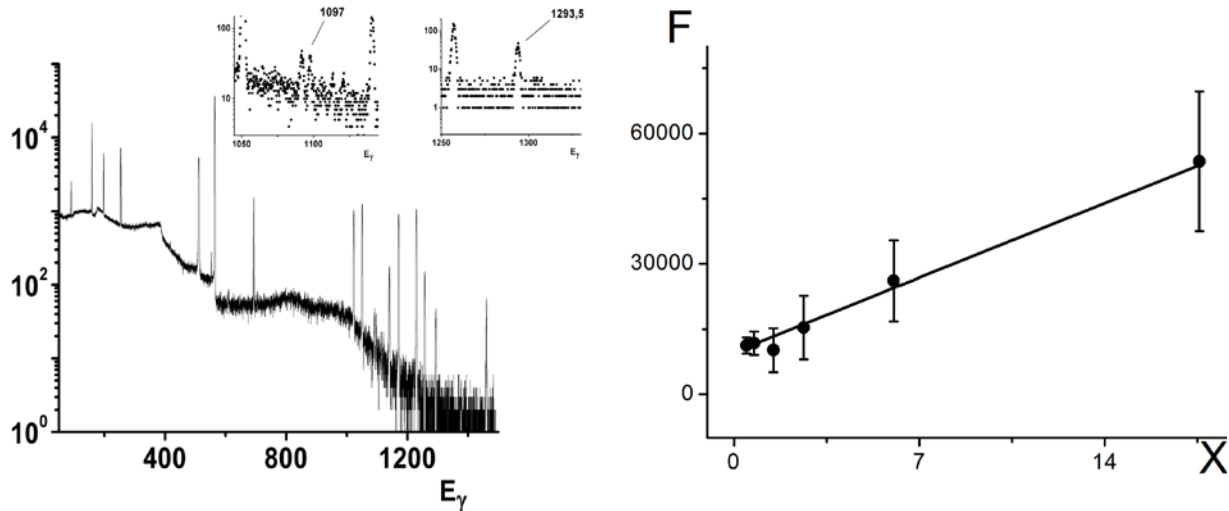
One can see (Fig. 1, right) the fitting result of the decay line in presentation (X, F) according to Eqs. (6, 7).

Gamma transitions and corresponding lines with the energies 1050.7 keV (EC+ $\beta^+$  decay of the isomer state) and 1229.7 keV (common line for decay of the ground and isomer states) were used to calculate the isomer ratio for  $^{118\text{m,g}}\text{Sb}$  (reaction  $^{121}\text{Sb}(\gamma,3n)^{118\text{m,g}}\text{Sb}$ ).

The gamma lines 1293.5 keV (common line EC+ $\beta^+$  decay of the ground and isomer state) were used to obtain the isomer ratio for  $^{116\text{m,g}}\text{Sb}$  (reaction  $^{121}\text{Sb}(\gamma,5n)^{116\text{m,g}}\text{Sb}$ ). The gamma line 1097 keV ( $\gamma$ -decay of the isomer state) were used to account contribution of  $^{116\text{m,g}}\text{In}$  (reaction  $^{121}\text{Sb}(\gamma,\alpha)^{116\text{m,g}}\text{In}$ ).

All obtained experimental values of the isomer ratios, corresponding reactions and characteristics of investigated nuclei are presented in Table 1.

The uncertainties given in table 1 include contributions from photopeak efficiency calibration, abundance, geometry configuration and intensities of gamma-rays (photopeak areas). Statistical uncertainties of photopeak areas made the main contribution to total uncertainty of result. Also number of experimental points of F,X dependency and range of X determination influenced total experimental error. These values were limited by experimental conditions.



**Figure 1.** Gamma-ray spectra from the antimony activities. The analytical gamma lines used for determination of the isomer ratios are indicated separately (left). Fitting line for experimental points (X, F) of antimony  $^{116m,g}\text{Sb}$  nuclei decay (reaction  $^{121}\text{Sb}(\gamma,5n)^{116m,g}\text{Sb}$ ) (right).

**Table 1.** Reactions, the bremsstrahlung energy end-points  $E_{\gamma\max}$ , spins of the target nuclei, spins of the meta-stable and ground states, the experimental isomer ratios  $IR=YH/YL$ , obtained in experiments.

Reaction	$E_{\gamma\max}$	$I_t$	$I_m$	$I_g$	$IR$
$^{121}\text{Sb}(\gamma,3n)^{118m,g}\text{Sb}$	38	5/2+	8-	1+	$0.14 \pm 0.04$
	43	5/2+	8-	1+	$0.14 \pm 0.01$
$^{121}\text{Sb}(\gamma,5n)^{116m,g}\text{Sb}$	53	5/2+	8-	3+	$0.25 \pm 0.03$

## Conclusion

Experimental values of the isomer ratios are obtained for  $^{118m,g}\text{Sb}$  and  $^{116m,g}\text{Sb}$  nuclei as products of the photonuclear reactions  $^{121}\text{Sb}(\gamma,3n)^{118m,g}\text{Sb}$  and  $^{121}\text{Sb}(\gamma,5n)^{116m,g}\text{Sb}$ , using bremsstrahlung endpoint energies in the region from 33 to 53 MeV. To correct deriving of isomer ratio for  $^{116m,g}\text{Sb}$  one must account the contribution of  $^{116m,g}\text{In}$  from reaction  $^{121}\text{Sb}(\gamma,n\alpha)^{116m,g}\text{In}$ .

## References

- Chadwick, M. B., P. Oblozinsky, P. E. Hodgson, G. Reffo. Pauli-blocking in the quasideuteron model of photoabsorption, *Phys. Rev.*, C44, 814–823, 1991.
- Dovbnya, A. N., M. I. Aizatsky, V. N. Boriskin, I. V. Khodak, V. A. Kusnir, V. V. Mytrochenko, A. N. Opanasenko, S. A. Perezhogin et al. Beam parameters of an S-band electron linac with beam energy of 30...100 MeV, *Problems of Atomic Science and Technology*, 2(46), 11–13, 2006.
- Gangrsky, Yu.P., A.P. Tonchev, N.P. Balabanov. Excitation of isomer states in photonuclear reactions, *PEPAN*, 27, 4, 1043–1098, 1996.
- Gokhale, P. A., S. Deokattey and V. Kumar. Accelerator driven systems (ADS) for energy production and waste transmutation: International trends in R&D, *Progr. in Nucl. Energy*, 48, 91–102, 2006.
- Herman, M., P. Oblozinsky, R. Capote et al. Recent Development of the Nuclear Reaction Model Code Empire, Proc. of International Conf. on Nuclear Data for Sci. and Technology “ND2004.” Sept. 26–Oct. 1, 2004. - Santa Fe (USA). N.-Y., AIP Conf. Proc., 769, 1184–1187, 2005.
- Ishkhanov, B.C., I.M. Kapitonov. *Interaction of electromagnetic radiation with nuclei*, M.: MSU, 215, 1979.
- Kolev, D., E. Dobрева, N. Nenov, V. Todorov. A convenient method for experimental determination of yields and isomeric ratios in photonuclear reactions measured by the activation technique, *Nucl. Instr. and Meth. in Phys. Res.*, A356, 390–396, 1995.
- Talou, P., T. Kawano, P.G. Young and M.B. Chadwick. The McGNASH nuclear reaction code and its use for gas production cross-section calculations, *Nucl. Instrum. Meth.*, A562, 823–826, 2006.
- Vanska., R., R. Rieppo. The experimental isomeric cross-section ratio in the nuclear activation technique, *Nucl. Instr. and Meth.*, 179, 525–532, 1981.
- WWW <http://higs.tunl.duke.edu>.
- WWW <http://www.nndc.bnl.gov/ensdf>.